



# Wireless Communications From the Ground Up

*An SDR Perspective*

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*In Loving Memory of My Mother*

*Rukhsana Jabeen*



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